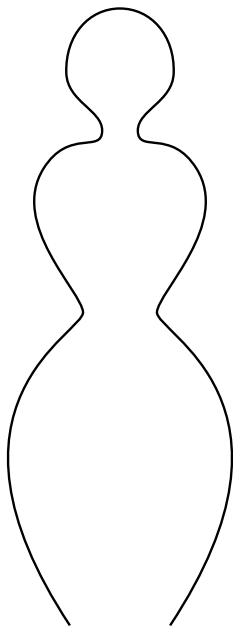


Ebenenbasiertes Kantenrouting mit Splines

Tibor Toepffer

27.08.2014

Schöne Kurven

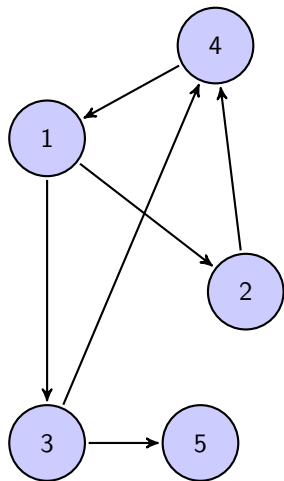


KLay Layered

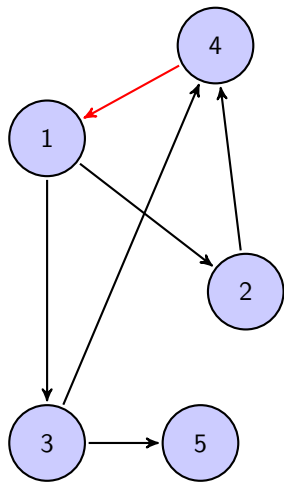
KLay Layered

Ebenbasiertes Layout von Graphen nach Kozo Sugiyama.

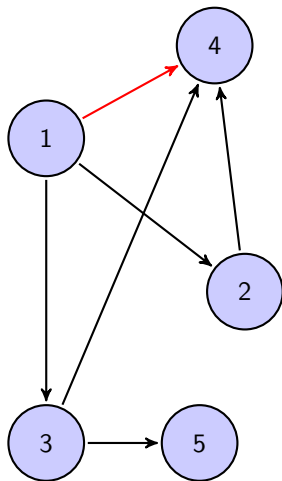
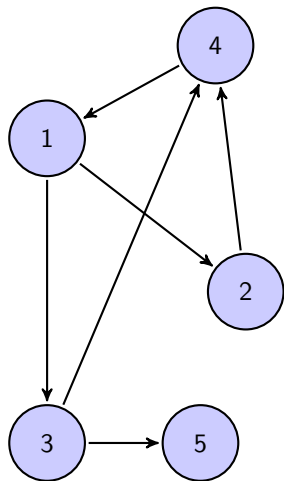
Phase 1: Zyklen auflösen



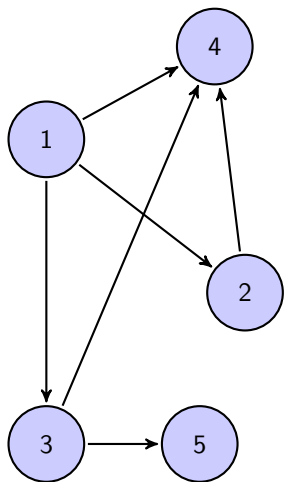
Phase 1: Zyklen auflösen



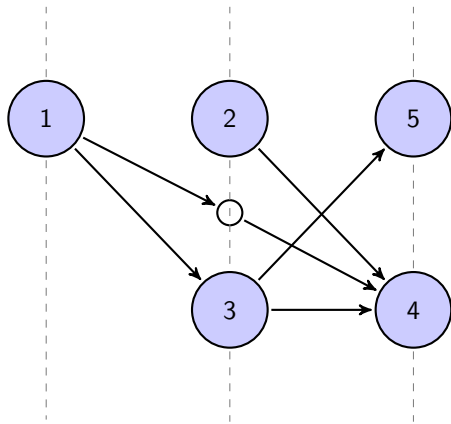
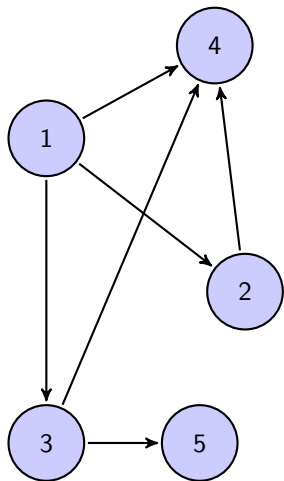
Phase 1: Zyklen auflösen



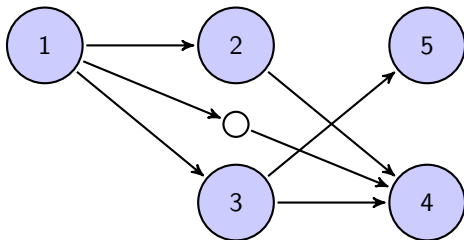
Phase 2: Knoten auf Ebenen verteilen



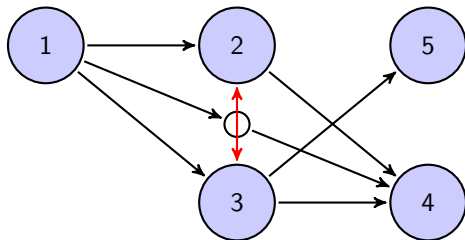
Phase 2: Knoten auf Ebenen verteilen



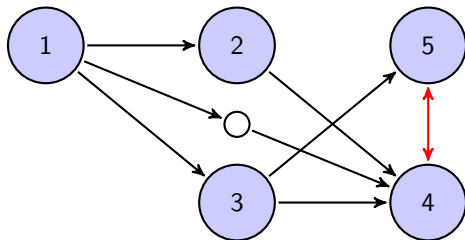
Phase 3: Kantenkreuzungen minimieren



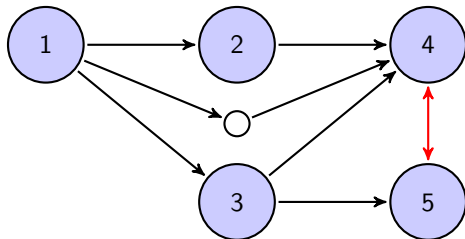
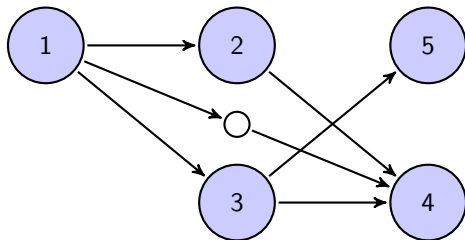
Phase 3: Kantenkreuzungen minimieren



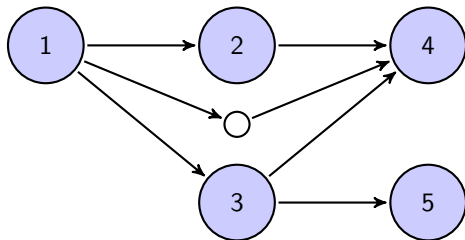
Phase 3: Kantenkreuzungen minimieren



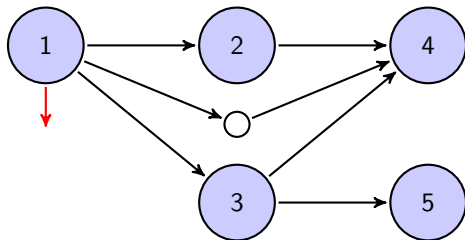
Phase 3: Kantenkreuzungen minimieren



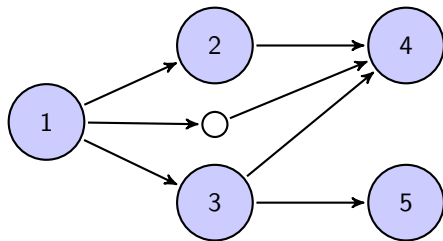
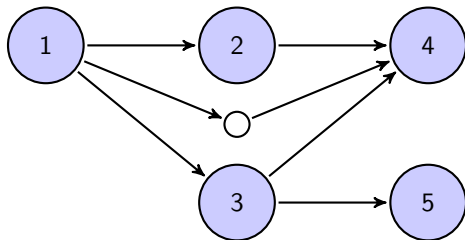
Phase 4: Vertikale Knotenposition festlegen



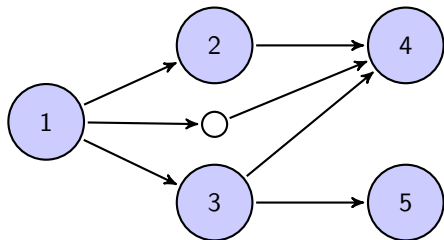
Phase 4: Vertikale Knotenposition festlegen



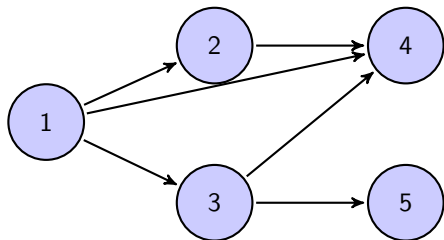
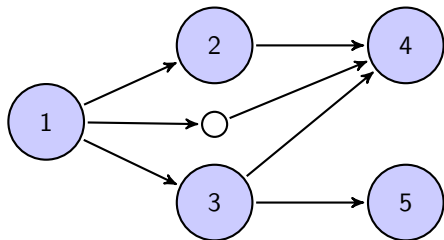
Phase 4: Vertikale Knotenposition festlegen



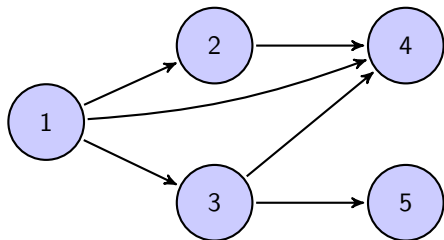
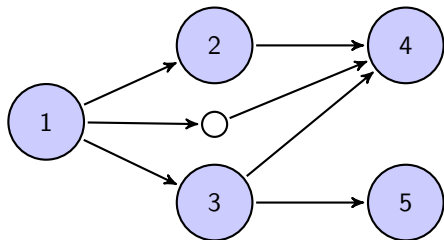
Phase 5: Kanten routen



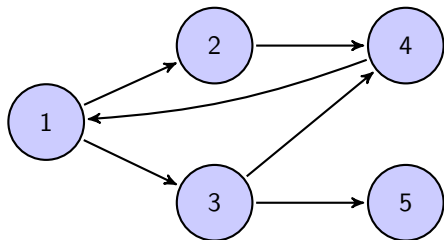
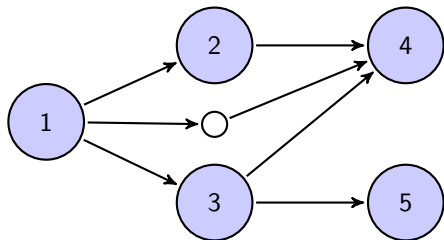
Phase 5: Kanten routen



Phase 5: Kanten routen



Phase 5: Kanten routen

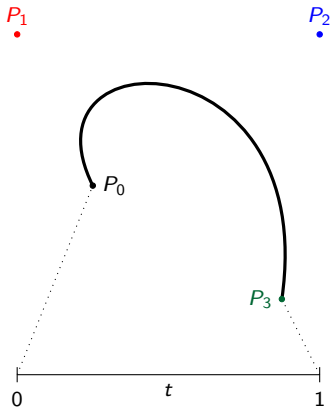


Erkenntnis vom letzten Vortrag?

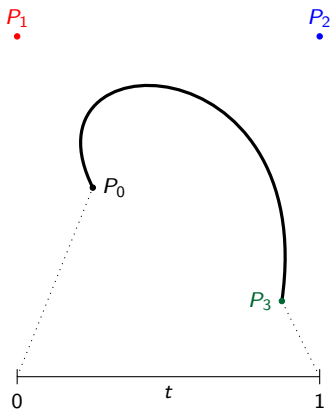
Erkenntnis vom letzten Vortrag?

Es gibt viele Arten von Splines!

Bezier-Kurven

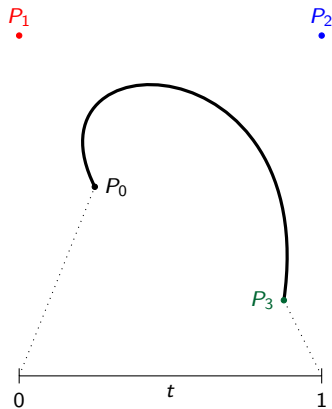


Bezier-Kurven

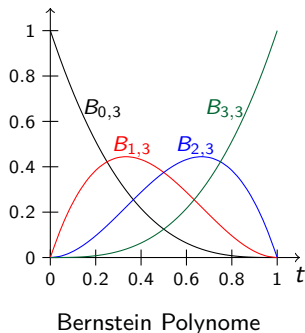


$$\text{Bezier}(t) = \sum_{i=0}^k B_{i,k}(t) \mathbf{P}_i$$

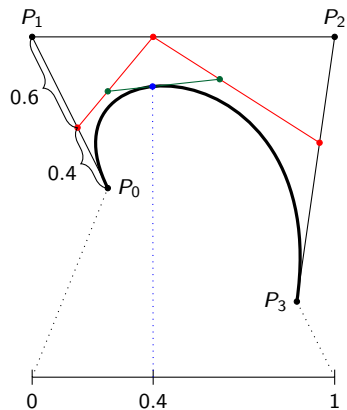
Bezier-Kurven



$$\text{Bezier}(t) = \sum_{i=0}^k B_{i,k}(t) \mathbf{P}_i$$

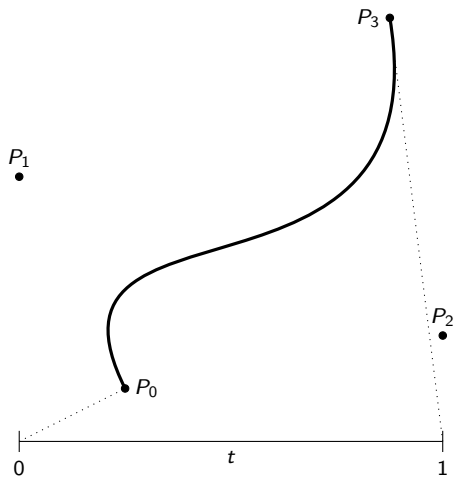


DeCastelau Algorithmus

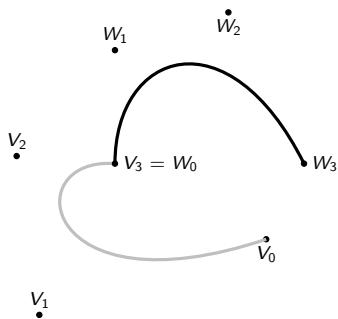


Beispiel für $t = 0.4$

Warum Splines?

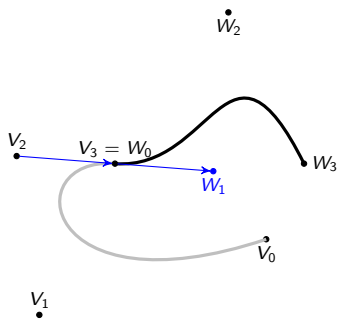


Bezier-Kurven \Rightarrow Bezier-Splines



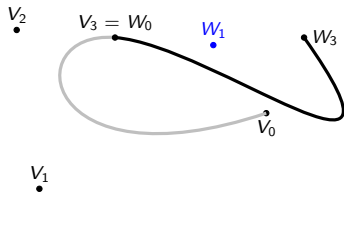
Stetig ersten Grades (C^1)

Bezier-Kurven \Rightarrow Bezier-Splines



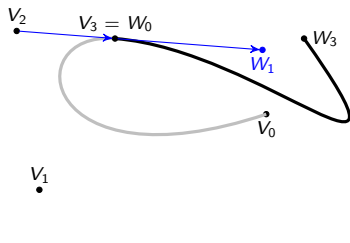
Stetig zweiten Grades (C^2)

Bezier-Kurven \Rightarrow Bezier-Splines



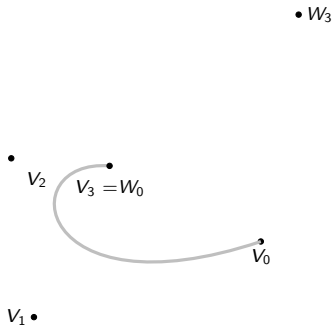
Stetig dritten Grades (C^3)

Bezier-Kurven \Rightarrow Bezier-Splines



Geometrisch Stetige (G^2)

β -Bezier-Kurven: Farin-Böhm Konstruktion

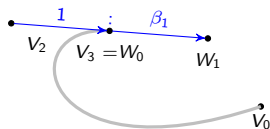


Freie Variablen:

- V_0, V_1, V_2, V_3, W_3

β -Bezier-Kurven: Farin-Böhm Konstruktion

• W_3

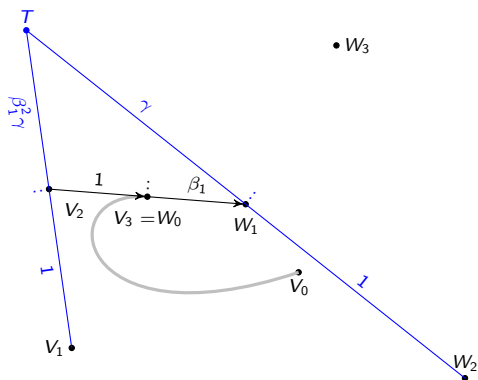


V_1 •

Freie Variablen:

- V_0, V_1, V_2, V_3, W_3
- $\beta_1 \in \mathbb{R}^{>0}$

β -Bezier-Kurven: Farin-Böhm Konstruktion

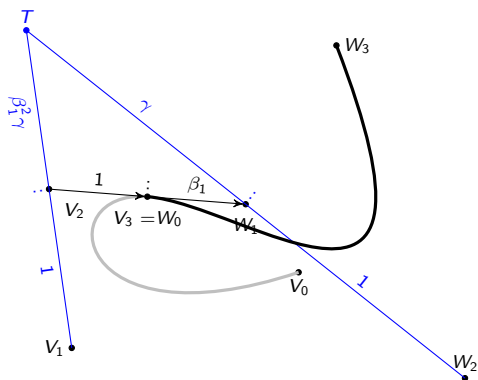


Freie Variablen:

- V_0, V_1, V_2, V_3, W_3
- $\beta_1 \in \mathbb{R}^{>0}$
- $\beta_2 \in \mathbb{R}$

$$\gamma = \frac{2(1 + \beta_1)}{\beta_2 + 2\beta_1(1 + \beta_1)}$$

β -Bezier-Kurven: Farin-Böhm Konstruktion

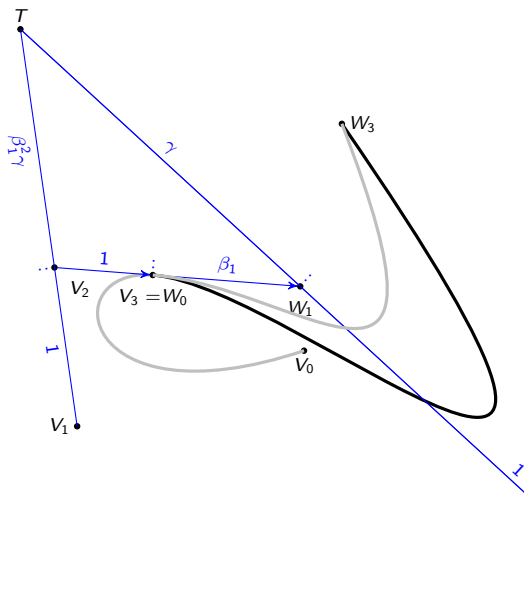


Freie Variablen:

- V_0, V_1, V_2, V_3, W_3
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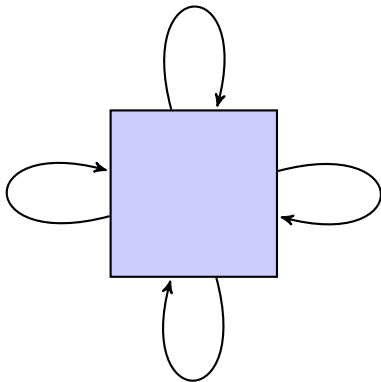
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- $\beta_2 \in \mathbb{R}$

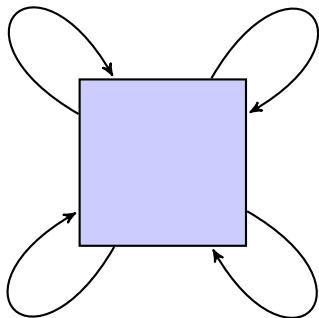
$$\gamma = \frac{2(1 + \beta_1)}{\beta_2 + 2\beta_1(1 + \beta_1)}$$

Self-Loops

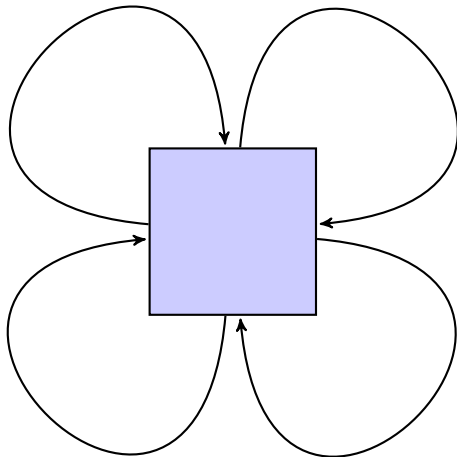
Self-Loops



Self-Loops

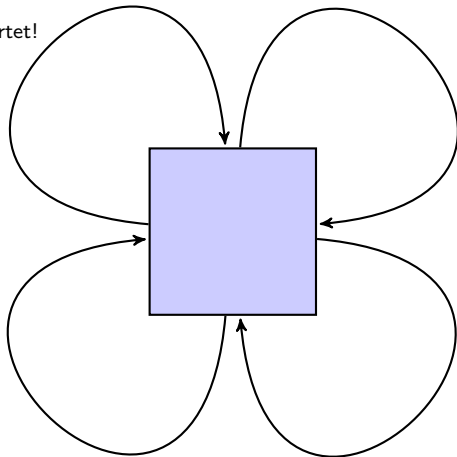


Self-Loops



Self-Loops

Besser als erwartet!



Jetzt neu: NURBS!

NURBS

Non-Uniform Rational B-Splines

$$\text{Bezier}(t) = \sum_{i=1}^k B_{i,k}(t) \mathbf{P}_i$$

NURBS

Non-Uniform Rational B-Splines

$$\text{Bezier}(t) = \sum_{i=1}^k B_{i,k}(t) \mathbf{P}_i$$

$$\text{NURBS}(t) = \frac{\sum_{i=1}^k N_{i,k}(t) w_i \mathbf{P}_i}{\sum_{i=1}^k N_{i,k}(t) w_i}$$

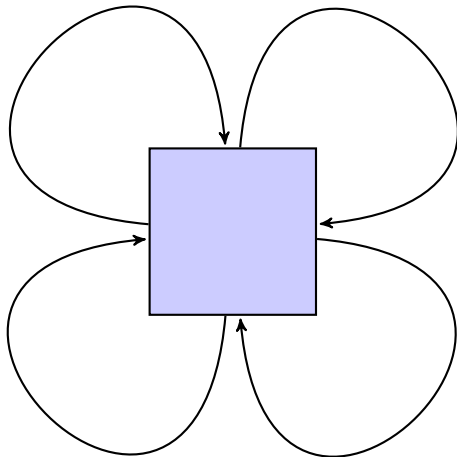
NURBS

Non-Uniform ~~Rational~~ B-Splines

$$\text{Bezier}(t) = \sum_{i=1}^k B_{i,k}(t) \mathbf{P}_i$$

$$\text{NUBS}(t) = \sum_{i=1}^k N_{i,k}(t) \mathbf{P}_i$$

Self-Loops mit NUBS



Fazit

- Splines gut geeignet

Fazit

- Splines gut geeignet
- Lokale Kontrolle wichtig

Fazit

- Splines gut geeignet
- Lokale Kontrolle wichtig
- ~~NUR~~BS die Technologie der Wahl

Fazit

- Splines gut geeignet
- Lokale Kontrolle wichtig
- ~~NUR~~BS die Technologie der Wahl
- In linearer Zeit in Bezier umrechenbar

Fazit

- Splines gut geeignet
- Lokale Kontrolle wichtig
- ~~NUR~~BS die Technologie der Wahl
- In linearer Zeit in Bezier umrechenbar
- Man muss loslassen können